Sampling

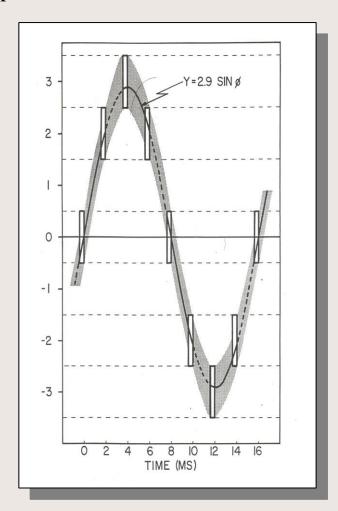
- Discrete sampling of continuous signals
- Binary representations of data
- Aliasing
- Dynamic range
- Reading:
 - > Telford et al., Sections 4.7.2-6

Discrete Sampling of Signals

- Suppose we need to digitize a continuous signal (vibration caused by a seismic source, gravity or electrical field, *etc.*).
- To design an Analogue-to-Digital (AD) converter, we have to answer two key questions:
 - 1. Choose the *sampling interval*. How dense the sampling should be?
 - 2. Choose the *dynamic range*. How *deep* should the amplitude measurement be? How many possible values should the discrete output contain?
 - ▶ In practice, these questions reduce to choosing a '8-bit', '16-bit', or '24-bit' AD converter.

Sampling and Quantizing Process

- Analog-to-Digital (AD) converter compares the levels of the signal to a set of predefined levels;
- Integer values are used as output;
- Need to have sufficient sampling density in *time* and *amplitude*.



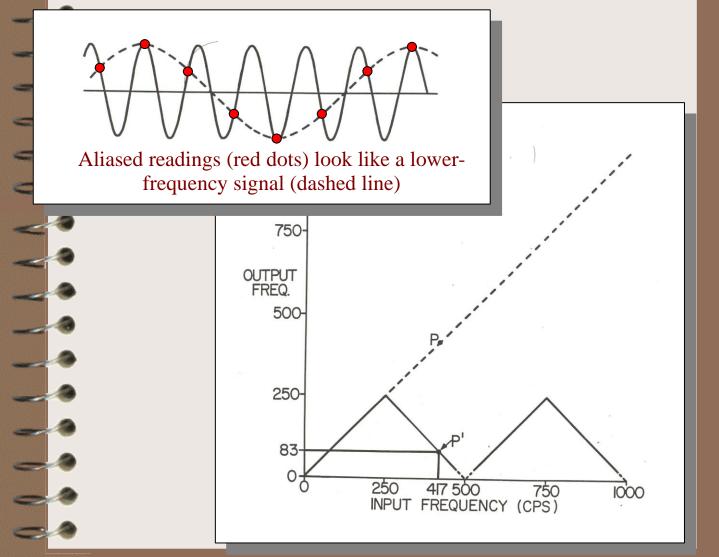
Nyquist Frequency

- Consider a seismic record sampled using N samples at a sampling interval of Δt . The fundamental frequency (the frequency of sampling) is then $1/\Delta t$
- However, it turns out that if we use less than two points per period T = 1/f, the signal can also be ambiguously represented by frequency $f_{\text{aliased}} = 1/(2\Delta t) f$ (see next slide)
- Consequently, the highest unambiguously recoverable frequency is $f_N = 1/(2\Delta t)$. This is called the *Nyquist frequency*
- Thus, the rule for choosing the sampling interval is: the shortest period of interest should include at least 2 samples.
 - In practice, twice faster sampling is typically used

Frequency Folding

(Aliasing)

- If sampling is attempted at frequency less than twice the frequency of the signal, distortion occurs (called *aliasing*)
 - High-frequency signal looks like low-frequency:



Aliasing

- Inadequate sampling rate results in *aliasing*: the signal above the Nyquist frequency appears as a distorted low-frequency signal.
- It is generally very difficult or impossible to clean up records contaminated with aliasing noise.
- To avoid aliasing, low-pass (called *anti-aliasing*) filters are built into the analogue parts of data loggers.

Binary representation of values

- All digital systems use binary system of representation of integer values.
 - ▶ Floating-point values are represented as three integers: *sign*, *mantissa*, and *exponent*.

Example:
$$-314.15 = -0.31415 \cdot 10^3$$
.

Exponent

Sign

Mantissa

- The binary scale uses only two digits, 0 and 1 (corresponding to a digital circuit states 'on' or 'off'). One element of this scale is called bit.
 - ♦ A series of 8 bits is called *byte*, bytes are arranged into *words*.
 - Typical AD converters output 1-, 2-, 3-byte (8-, 16, 24-bit) words.
- Each additional bit doubles the range of possible output values.
 - Here is how the decimal value of 101is represented by a 8-bit binary word 01100101:

27	26	2 ⁵	2^4	23	22	21	20	
0	1	1	0	0	1	0	1	
0	64	32	0	0	4	0	1	

Dynamic Range

- The 'depth' of magnitude recording is measured by its *dynamic range*, expressed in decibels (dB)
 - → Dynamic range measures <u>the ratio</u> of the maximum and minimum amplitudes that are (or can be) correctly recorded.

$$\left(\frac{A_1}{A_2}\right)_{\text{in dB}} = 20\log_{10}\left(\frac{A_1}{A_2}\right)$$

- In a digital recorder, the dynamic range is controlled by the *number of bits* used to store or output the values.
 - Each additional bit allows doubling the recorded values; thus, it corresponds to additional $20\log_{10}2 = 6dB$.
 - Modern data loggers use 24-bit AD converters; this gives about 140 dB of dynamic range