

Geol 335.3

Lab #4: Seismic Modelling

In this lab, you will study the response of the direct, reflected and refracted waves in a simple layered Earth model, and generate a simple seismic plot using Matlab or Octave. The three-layer and a half-space model is given in the following table:

Layer	Thickness (m)	Velocity (m/s)
1	100	450
2	200	2000
3	200	3000
4	∞	6000

Copy to yourself and unpack the [zipped archive](#). Modify the examples in script lab4.m (or create your own). In this

Let us simulate a seismic survey conducted over this layered structure with the following specifications:

- Source located at $x = 0$;
- Receivers located from $x = -1000$ m to 1000 m;
- Spacing between receivers 10 m.

This layout can be described in Matlab by writing:

```
x_source = 0.0;           % source position
x = -1000:10:100;        % geophone positions
```

The modelling function `trefr(...)` provided in the lab is most convenient to use if the depth/velocity model is provided in the form of arrays. The model above can then be described in two Matlab variables:

```
h = [ 100, 200, 200 ];           % layer thicknesses
v = [ 450, 2000, 3000, 6000 ];   % layer velocities
```

With these initial settings, perform the following modelling steps:

Task (1) (10%) **For each velocity contrast in the model, determine:** a) critical ray parameters; b) critical distances, c) intercept times for the refractions, d) t_0 times and RMS velocities for the reflections. In Matlab, assign identifiers to these quantities, such as:

```
p_crit_1 = ...;           % critical ray parameter
```

```

x_crit_1 = ...;    % critical distance
t_int_1 = ...'    % intercept time
t_int_2 = ...;
t0_1 = ...;      % normal-incidence reflection time;
v_rms_1 = ...;

```

and so on. In the following, use these identifiers rather than constants.

Note: the units for distance should be m, time – ms, velocity – accordingly, m/ms (or km/s).

Task (2) (25%) Using Matlab, **compute the arrival times** of the direct, reflected and refracted waves from all the acoustic discontinuities for all receivers. Plot these arrival times on a common T-X graph. It would be helpful to write two Matlab *functions* to calculate reflection and refraction travel times, respectively:

```
trefl(t0,v_rms) and trefr(t_intercept,v_refractor)
```

In the subsequent steps, you will simply use e functions instead of retyping the formulas.

Next, look into the function `wavelet_ft(t)`. This function returns a wavelet (array) of amplitude 1.0, centred at time $t=0$ and discretized at times specified in array 't' (in milliseconds). The wavelet is obtained by summation of 81 cosine waves of amplitude $1.0/81.0$, with frequencies from 20 Hz to 60 Hz with a 0.5 Hz interval¹. Finally, the waveform is multiplied by a sine “taper” function to ensure that its values at the ends of the time interval equal zero.

The obtained wavelet is your *source signature* (aligned at 0 ms time). Such symmetric with respect to time = 0 waveforms are called “zero-phase”.

Task (3) (10%) Test function `wavelet_ft()` and **precompute the source waveform** for 30-Hz dominant frequency by executing something like this:

```

global tref wref

tref = -500:1:500;
wref = wavelet_ft(tref,30);
plot(tref,wref,'b-')
xlabel('Time (ms)')
ylabel('Displacement')
title('Wavelet at 30 Hz')
save wavelet.mat tref wref

```

¹ We will return to this procedure of constructing pulses from sinusoidal functions when studying Fourier transforms in the lectures and lab 7.

These commands create an array of times `tref` centred at `t=0`, model wavelet `wref` on it, plot `wref`, and save it in a file. This precomputed wavelet can be loaded like this:

```
global tref wref
load wavelet.mat
```

This `.mat` file will be used later in this and other labs.

Task (4) (10%) Look into the second Matlab function `wavelet(a0, t0, t)`. This function uses the precomputed `tref` and `wref` and returns the same wavelet but with arbitrary amplitude '`a0`' and centred at arbitrary time '`t0`' [ms]. The output is obtained by linear interpolation (function `interp1(...)`), and this function works is much faster than the cosine-wave summations above.

Test this function like this (you can change parameter values to achieve nice plots):

```
t = 0:2:1000;
plot(t, wavelet(5.0, 100.0, t) );
```

Print out the resulting plot out and indicate whether the time and amplitude of the waveform are as expected.

Task (5) (40%) Using the calculated arrival travel-times and `wavelet(...)` function, **use Matlab to plot a *shot gather*** – a set of seismic traces simulated at each of the 100–200 geophone locations.

For time sampling in the plots, use 0–1200 ms time range, at 2 ms intervals:

```
t = 0:2:1200;    % time sampling
```

Note that the provided function `trefl(...)` (modelling reflection times) uses an approximation which is accurate only for the single-layer case. Therefore, model reflections only from the uppermost boundary. As a result, you should have five waves in your section:

- Direct wave through the first layer;
- Three head waves from each refracting boundary;
- Reflection from the top of the second layer.

For plotting, you use Matlab's `hold on` command (to prevent from starting a new display window on every `plot()` call) and arrange a loop over the receivers:

```
figure(1)
clf          % clear the figure in case it gets reused
```

```

hold on

for i=1:numel(x)

    % place the plotting commands for i-th receiver
    % (see below) here ...

end

```

In this loop, first determine the offset, then the travel for each wave, and then attach a wavelet to this travel time. Sum the waveforms in a common array `trace`, which will simulate the seismic record:

```

% determine the source-receiver distance for this trace
offset = abs(x(i) - x_source);

% put direct wave into new trace
trace = wavelet(amp, offset/v(1), t );

% add reflection from the first interface
trace = trace + wavelet(amp, trefl(t0_1,v_rms1, offset), t );

% add into 'trace' refraction from the first interface

if x > x_crit_1
    trace = trace + wavelet(amp, trefr(t_int_1,v(1)), t );
end

% ... from the second interface:

if x > x_crit_2
    trace = trace + wavelet(amp, trefr(t_int_1,v(1:2)), t );
end

% ... and similarly for the third interface ...

% plot the resulting seismic trace:
plot(trace+x,t);

```

Here, `t_direct`, `t_head`, and `t_reflected` should be the times of your arrivals.

The horizontal axis of the plot will become the distance, and the shifts of `x` added to the 'trace' values will place your wiggles ("traces") at the positions of geophones. Parameter `amp` becomes trace excursion (swing amplitude) and should be selected so that the plot looks nice (I suggest ~15-20).

Time should be plotted along the vertical axis downward, as it is commonly done in refraction/reflection record sections. This direction of the axis can be achieved in Matlab by command

```
set(gca,'ydir','reverse');
```

Task (6) (5%) **Note the interference (overlap)** between the different waves near critical and crossover distances, and at far offsets. **Mark these interfering events in your section.** Comment on the tuning effects (enhancement or cancellation of arrival amplitudes) as they approach each other within a dominant period.

Theory:

The cosine function of amplitude A , frequency f , and centered at time t_0 (used in `wavelet_ft()`) is:

$$u(t) = A \cos(2\pi f(t - t_0))$$

For a stack of layers, travel time of the reflection from the bottom of n -th of them is given by the same formula as within a single layer:

$$t(x) = \sqrt{t_0^2 + \left(\frac{x}{V_{RMS}}\right)^2},$$

where t_0 is the vertical-incidence travel time, and V_{RMS} is the effective (average, “root-mean-square”) velocity of the stack of layers:

$$V_{RMS}^2 = \frac{\sum_{i=1}^n V_i^2 \Delta t_i}{\sum_{i=1}^n \Delta t_i},$$

where $\Delta t_i = \Delta z_i / V_i$ is the vertical travel time for each layer.

Hand in:

Code printouts, plots, and comments on paper or by email (zipped or merged in a Word, PDF, or PowerPoint file).